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Repeated weighting in mixed-mode censuses¹

Marcin Szymkowiak², Kamil Wilak³

Abstract: The main aim of the paper is to use the repeated weighting (RW) method on data from the National Census of Population and Housing 2011 (NCPH) and Labour Force Survey (LFS) to ensure consistency between margins of final tables derived from different statistical sources. This technique, based on different data sources, would ensure consistency between estimates in final output tables. This is the first application of the RW approach on data from official statistics in Poland. The results obtained by applying the RW method to data from the NCPH and additional surveys (e.g. LFS) may be used by Statistics Poland for the formulation of conclusions and recommendations for the upcoming census in 2021. The method may be also considered as an important step towards the production of timely and more detailed statistical information in Poland based on multi-source data infrastructure in general⁴.

Keywords: repeated weighting method, calibration, Generalised Regression Estimator, data linkage, National Census of Population and Housing 2011, Labour Force Survey.

JEL codes: C13, C83, J21.

Introduction

Weighting is a statistical technique commonly used and applied in practice to compensate for nonresponse and coverage errors (Särndal & Lundström, 2005). It is also used to make weighted sample estimates conform to known popula-

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⁴ The views expressed in this paper are those of the authors and do not necessarily reflect the policies of Statistics Poland.

tion external totals. In recent years a lot of theoretical work has been done in the area of weighting and there has been a rise in the use of these methods in many statistical surveys conducted by National Statistical Offices around the world (Särndal, 2007). One of the most common techniques of weighting is calibration, which is a method of adjusting initial weights in surveys based on sampling in order to estimate known population totals of all auxiliary variables perfectly (Deville & Särndal, 1992). This method can also be used in surveys as a possible way of tackling unit nonresponse, providing gains in efficiency in terms of variance when there is a strong correlation between the variable of interest and auxiliary variables (Lundström & Särndal, 1999; Kott, 2006; Kott & Chang, 2010). It is worth noting that calibration is one of many weighting methods that can be used in practice. Others include poststratification, raking, GREG weighting (Generalised Regression Estimator), logistic regression weighting, mixture approach and logit weighting. A review of the weighting method with examples can be found in Kalton and Flores-Cervantes (2003).

However, in practical applications, the calibration approach is often faced with a well-known problem: the inclusion of too many auxiliary variables may have several negative consequences (Szymkowiak, 2019). In particular, the use of too much auxiliary information may result in unstable estimates due to a large number of regression coefficients that have to be estimated from the sample. This problem is especially evident when an attempt is made to estimate a large set of tables from several data sources (sampling surveys, registers) in order to ensure that all estimates are mutually consistent, i.e. corresponding margins of any two estimated tables are equal (Boonstra, 2004). To obtain consistent estimates, Rennsen, Kroese and Willeboordse (2001) proposed a procedure of repeated weighting. This technique involves repeated application of the generalized regression estimator and generates a new set of weights for each table, which is estimated in order to achieve numerical consistency for margins of all tables. It is worth mentioning that so far the RW method has been successfully used only by Statistics Netherlands in their virtual census which is a set of integrated microdata files with coherent and detailed demographic and socio-economic data on persons, households, dwellings, jobs and benefits.

When data from different sources have to be reconciled the RW method may be considered (De Waal, Delden, & Scholtus, 2020). This statistical technique was developed for situations where information on one or several variables is available from more than a single data source (e.g. from administrative registers and sample surveys). The purpose of RW is to create appropriate weights for predefined census tables in order to ensure consistency of margins of all tables created with the use of various data sources supplying the census. This approach is in line with the growing need of linkage multiple data sources reported by National Statistical Institutions (NSIs) (Harron, Goldstein & Dibben, 2015). Nowadays data linking is an important cornerstone in the production of statistical information. Applications that use linked data are also a part of

mainstream social science research (Chambers & Diniz da Silva, 2020). Thanks to data linkage NSIs may avoid increasing the respondent burden. Moreover, another advantage of data linkage is the possibility of producing statistics with a higher degree of granularity than is typically the case in normal statistical procedure of data production (Luppes & Nielsen, 2020). It means that by combining data sources statistical agencies are able to produce more detailed and more timely statistics than using any single data source alone (Yang & Kim, 2020).

In the light of the above, the main aim of the study described in this article is to apply the RW method using data from the National Census of Population and Housing 2011 and the Labour Force Survey in order to ensure consistency of margins in the final tables. This article is organized as follows. Section 1 introduces the methodology of repeated weighting, including a brief description of the Generalised Regression Estimator which is the underlying concept of RW. Section 2 provides an overview of data from the National Census of Population and Housing 2011 and the Labour Force Survey in Poland. Finally, in Sections 3 and 4 the applications and results of the RW approach on data from official statistics in Poland are discussed. The paper ends with some concluding remarks.

1. Repeated weighting—theoretical aspects

With regard to sample surveys conducted by national statistical offices all over the world, it is assumed that each survey is carried out independently of the others. Therefore, a unique system of weights is created for each survey, which is used in the process of generalizing the results at the level of the entire population or for appropriately defined domains.

The final set of weights constructed for a given survey is used to create consistent tables but only within that particular survey. The situation becomes more complicated when multidimensional tables are created containing variables from more than one survey. Because of different systems of weights the final tables obtained from different surveys may not be consistent. This issue is particularly undesirable when one considers expectations of users of statistical data where it would be difficult to accept the situation of having different estimates of margins in the final tables for a variable defined in the same way in two different surveys relating to the same reference period.

Recognizing the problem outlined above, Statistics Netherlands implemented an estimation strategy alternative to calibration, referred to as the repeated weighting method, which aims to ensure consistent estimates for tables constructed with the use of data from various sources. This method has been described in several papers but its basic concept was formulated in Kroese and Rensen (1999). The method has been later developed theoretically and its practical applications have been described in Boonstra, van den Brakel, Knottnerus,

Nieuwenbroek and Renssen (2003), Houbiers, Knottnerus, Kroese, Renssen and Snijders (2003), Houbiers (2004) or Boonstra (2004). The construction of the variance estimator in the repeated weighting method is described in detail by Knottnerus and van Duin (2006), while the process of applying the RW method in a virtual census is discussed by Nordtholt (2005) in the context of the 2001 census and by Nordtholt, Zeijl and Hoeksma (2014) in relation to the 2011 census.

The main purpose of the repeated weighting method is to obtain a set of consistent tables when the counts are estimated using data from various sources (e.g. registers and selected sample surveys). Consistency of all tables means that margins for the same variables that can occur in at least two data sources used in the analysis are perfectly equal.

The repeated weighting method is based on the following four assumptions (Knottnerus & van Duin, 2006):

- 1) the reference period of the registers and surveys is the same;
- 2) the registers and surveys refer to the same population;
- 3) variables with the same name have the same definition for all relevant registers and surveys;
- 4) the categorical variables have hierarchical classifications, i.e. each class of a more detailed classification is nested within one class of a less detailed classification.

The repeated weighting method proposed by Statistics Netherlands consists of three main steps which can be synthetically described by the following algorithm.

In order to describe in detail this algorithm of the repeated weighting method a scenario with three data sources will be considered: a full enumeration (*FE*) and two sample surveys (*SS1*, *SS2*) (see Figure 1).

In Figure 1 block S_0 corresponds to the full enumeration *FE* which covers the entire population and include variables *A*, *B*, *C*. Block S_1 consists of respondents from the sample survey *SS1* and includes variables *A*, *B*, *C*, *D* from both *FE* and *SS1*. Similarly block S_2 includes respondents from the sample survey *SS2* and variables *A*, *B*, *C*, *E* from *FE* and *SS2*. Block S_3 contains units that were covered simultaneously by both sample surveys *SS1* and *SS2* and contain variables *A*, *B*, *C*, *D*, *E* from all three surveys *FE*, *SS1* and *SS2*.

As mentioned in Algorithm 1, the first step involves specifying the output tables in which appropriate counts are subject to the estimation process. Then, for the output tables defined in this way, their margins are added. The margins in a table are obtained by (i) aggregating the counts of one or more categorical variable of a multivariate table or by (ii) using less defined variants of the categorical variable. For example, two-dimensional table $D \times E$ contains margins for table $C \times D \times E$, but also for table $D \times E^{(2)}$, where variable $E^{(2)}$ has fewer levels than variable *E* and levels of variable $E^{(2)}$ are obtained by aggregating levels of variable *E*. The tables are then ordered in the estimation process in such a way that the table with margins always precedes the more complex one.

Algorithm 1. Repeated weighting method**Step 1:** *Specification of output tables*

Define all final tables and degree of nesting for individual variables.

Step 2: *GREG estimation of the tables*

Estimate the counts in tables using the generalized linear regression estimator and the most appropriate data set.

Step 3: *Recalibration (the reweighting step)*

Ensure numerical consistency between margins for different tables i.e. make sure that the margins of the reweighted table are consistent with their estimates from a preceding table or their known counts from a register.

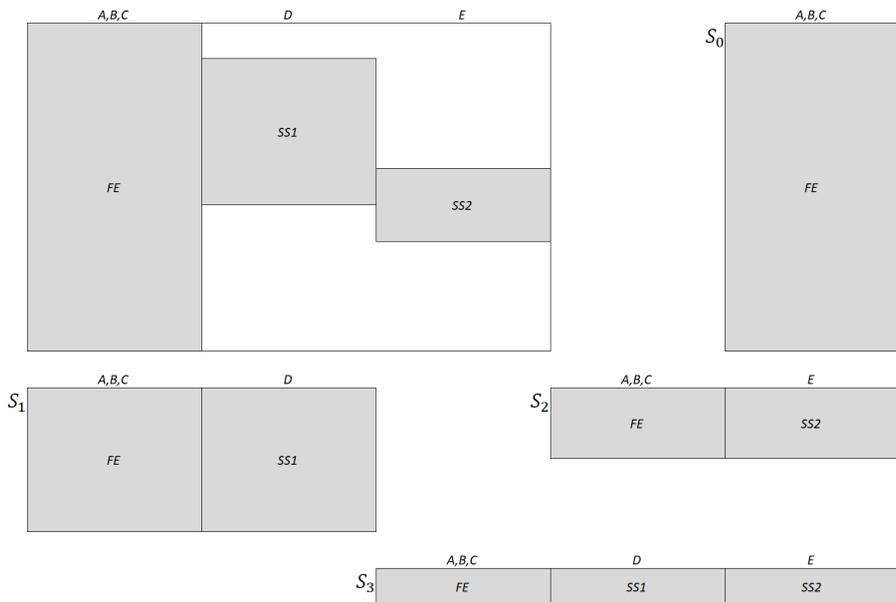


Figure 1. An illustrative set of surveys and the construction of blocks

Source: Based on (Knottnerus and van Duin, 2006).

In the second step of Algorithm 1 the counts in each specified table are estimated using the generalized linear regression estimator (GREG)⁵ and the most appropriate data set, which is called a block and is denoted by S . In most cases it will be the biggest survey in terms of sample size or a combination of surveys containing the variables required to derive the output variable. For example, if one wants to construct a two-dimensional table including the counts for levels of variables C and D , the S_1 block should be used, as presented in Figure 1.

⁵ Other calibration estimators based on different distance functions may be applied. Examples of such distance functions may be found in Deville and Särndal (1992), Haziza and Lesage (2016) or Wu and Lu (2016).

At this point, it should be emphasized that if all variables used in the process of constructing a table come from the register (in the case of the example shown in Figure 1, say, table $A \times B \times C$) then there is no need to estimate the appropriate counts. In this situation the table is built by simply summing up the counts for levels of individual variables in the register.

Let $\mathbf{x}_k = (x_{k1}, \dots, x_{kJ})^T$ denote a vector composed of values of auxiliary variables for the k -th unit, where J denotes the number of auxiliary variables, and k denotes units in the appropriate S block, i.e. $k \in S$. Moreover let $\boldsymbol{\tau}_X = \sum_{k \in U} \mathbf{x}_k$ denote a vector composed of totals of all auxiliary variables, and $\boldsymbol{\tau}_Y = \sum_{k \in U} \mathbf{y}_k$ – a vector composed of the numbers in the appropriate cells of the multidimensional table corresponding to a categorical variable Y that has P mutually exclusive levels. The vector \mathbf{y}_k corresponding to $\boldsymbol{\tau}_Y$ can then be perceived as a P -dimensional vector consisting of all zeros except for one unit value denoting the fact of belonging to the appropriate class of the k element in relation to the categorical variable Y . Assuming the above notation the estimator of $\boldsymbol{\tau}_Y$ can be defined as follows:

$$\hat{\boldsymbol{\tau}}_Y^{GREG(S)} = \hat{\boldsymbol{\tau}}_Y^{HT(S)} + \hat{\boldsymbol{\beta}}_S^T (\boldsymbol{\tau}_X - \hat{\boldsymbol{\tau}}_X^{HT(S)}) = \sum_{k \in S} d_k^{(S)} \mathbf{y}_k + \hat{\boldsymbol{\beta}}_S^T \left(\boldsymbol{\tau}_X - \sum_{k \in S} d_k^{(S)} \mathbf{x}_k \right), \quad (1)$$

where:

$$\hat{\boldsymbol{\beta}}_S = \left(\sum_{k \in S} d_k^{(S)} \mathbf{x}_k \mathbf{x}_k^T \right)^{-1} \sum_{k \in S} d_k^{(S)} \mathbf{x}_k \mathbf{y}_k^T, \quad (2)$$

and $\hat{\boldsymbol{\tau}}_Y^{HT(S)}$ and $\hat{\boldsymbol{\tau}}_X^{HT(S)}$ denote estimates obtained by using a well-known Horvitz-Thompson (HT) estimator for data from the S block.

The weights $d_k^{(S)}$ in formulas (1) and (2) are selected because of the construction of the S block. Given this setup (see Figure 1), two situations are possible:

1. S is the same as the sample selected in one of the sample surveys: in this case, the weights from this survey are used as weights $d_k^{(S)}$ ⁶;
2. S is the common part of two blocks S_1, S_2 corresponding to two sample surveys, i.e. $S = S_1 \cap S_2$; then the weights are constructed as the product of the weights from both surveys:

$$d_k^{(S)} = d_k^{(S_1)} d_k^{(S_2)}, \quad (3)$$

which corresponds to the inverse of the probability that the k -th unit was selected for both surveys.

⁶ These can be the original weights but, in practice, they tend to be calibration weights.

The generalized regression estimator of the form (1), which is used in the repeated weighting method in the second step of Algorithm 1 can also be written in an equivalent way:

$$\hat{\boldsymbol{\tau}}_Y^{GREG(S)} = \sum_{k \in S} w_k^{(S)} \mathbf{y}_k \quad (4)$$

where weights $w_k^{(S)}$ can be expressed as follows:

$$w_k^{(S)} = d_k^{(S)} \left\{ 1 + \mathbf{x}_k^T \left(\sum_{k \in S} d_k^{(S)} \mathbf{x}_k \mathbf{x}_k^T \right)^{-1} (\boldsymbol{\tau}_X - \hat{\boldsymbol{\tau}}_X^{HT(S)}) \right\}. \quad (5)$$

It may happen that the margins for a table estimated in the second step do not match the values in the previously created table in terms of shared variables. In this case, it is necessary to recalibrate the estimates to ensure the consistency of the estimated tables, which is exactly what happens in the third step of the RW method. Recalibration should therefore be understood as the process of adjusting values of a more detailed table to ensure that its margins are consistent with the margins of the previous table. For this purpose, the GREG estimator is used again.

Let \mathbf{m} denote a vector of all linearly independent auxiliary variables corresponding to the margins of a table whose counts are contained in $\boldsymbol{\tau}_Y$. The estimator of the parameter $\boldsymbol{\tau}_Y$, based on the data from the S block, which is obtained in the third step of the RW method can be expressed as follows:

$$\hat{\boldsymbol{\tau}}_Y^{RW} = \hat{\boldsymbol{\tau}}_Y^{GREG(S)} + \hat{\boldsymbol{\beta}}_{S,RW}^T (\hat{\boldsymbol{\tau}}_m^{RW} - \hat{\boldsymbol{\tau}}_m^{GREG(S)}) \quad (6)$$

where:

$$\hat{\boldsymbol{\beta}}_{S,RW} = \left(\sum_{k \in S} w_k^{(S)} \mathbf{m}_k \mathbf{m}_k^T \right)^{-1} \sum_{k \in S} w_k^{(S)} \mathbf{m}_k \mathbf{y}_k^T. \quad (7)$$

The elements of the vector $\hat{\boldsymbol{\tau}}_m^{RW}$ are estimates from the previous table or known counts from the register. Also, in this case, the estimator of the RW type, which is expressed by formula (6), can be represented in an alternative form using appropriate weights, i.e.:

$$\hat{\boldsymbol{\tau}}_Y^{RW} = \sum_{k \in S} r_k^{(S)} \mathbf{y}_k \quad (8)$$

where:

$$r_k^{(S)} = w_k^{(S)} \left\{ 1 + \mathbf{m}_k^T \left(\sum_{k \in S} w_k^{(S)} \mathbf{m}_k \mathbf{m}_k^T \right)^{-1} (\hat{\boldsymbol{\tau}}_m^{RW} - \hat{\boldsymbol{\tau}}_m^{GREG(S)}) \right\}. \quad (9)$$

Another important issue in the repeated weighting method is the way of estimating the variance of the $\hat{\tau}_Y^{RW}$ estimator. How this variance estimator is constructed is described in the article by Kottnerus and van Duin (2006), in which the authors focus on the case of one register and two independent sample surveys.

To conclude this section, it is worth emphasizing that the repeated weighting method is not the only technique that can be used in the process of constructing tables that preserve the consistency between respective margins. Some alternatives to the RW method include imputation-based approaches (mass imputation, the repeated imputation technique) and macro-integration. They are described in detail in De Waal (2016).

2. The data

In order to present the possibility of using the repeated weighting method in the NCPH and to construct appropriate census tables, data from the Labour Force Survey were additionally considered. The main objective of the LFS is to collect information about the working, unemployed and economically inactive population. Because the reference point of the NCPH was March 31, 2011, LFS data from for the first quarter of 2011 were used in the analysis (85,275 observations).

NCPH 2011 was a mixed mode census, i.e. based on data from administrative sources as well as those collected directly from the population, partly by full enumeration and partly through a sample survey (Statistics Poland, 2014). Collected information about permanent residents living in Poland is contained in two datasets: one with 31,957,682 observations from full enumeration and the second one, with 6,694,220 records, from the sample survey.

The repeated weighting method requires that data from different sources supplying a census (registers and sample surveys) are properly linked. Deterministic or stochastic methods of data linkage may be used to combine information from different sources to identify and bring together records from separate files, which correspond to the same entities (Rässler, 2012; Roszka, 2013). In most cases, it is not a simple procedure and linkage errors, false and missed links are unavoidable (Zhang & Tuoto, 2020).

In the deterministic method unique identifiers for each record are compared to determine a match (Harron et al., 2015). In administrative sources relating to persons the PESEL number (Universal Electronic System for Registration of the Population in Poland) is typically used as the matching key. In practice, however, it often happens that there is no common key in datasets to be linked. In such situations stochastic methods are used, including probabilistic record linkage which makes it possible to integrate databases containing information about the same units with no shared unique key (Sayers, Ben-Shlomo, Blom

& Steele, 2016). This method uses the so-called pairing variables, which are used to estimate the probability that a pair of records from different datasets refer to the same unit. Pairing variables are selected from among the variables present in both integrated datasets; in the case of persons, likely candidates include the address of residence, sex or birth date.

Owing to the lack of access to unique identifiers shared by the NCPH and the LFS deterministic integration could not be used. This is why probabilistic record linkage, mentioned above, was applied. In order to optimize the integration algorithm by reducing the number of record pairs to be compared, the following variables were used as blocking variables: the commune of residence (NUTS5 level), the category of the place of residence (urban / rural), sex and ten-year age groups. Record matching was performed using the birth year as a pairing variable. The reclin package (van der Laan, 2018) of the R program (R Core Team, 2019) was used for the stochastic process of data integration.

Following the integration only some respondents in the LFS (18,481 observations) were linked with both the full and sample part of the NCPH (see Figure 2). A much larger group of LFS respondents could only be linked with the full part of the NCPH (66,794 observations). The inclusion relationship between sets *FS*, *SS1*, *SS2* will be used for the construction of the so-called blocks, i.e. sets that will be the basis for estimating total values in the specified output tables.

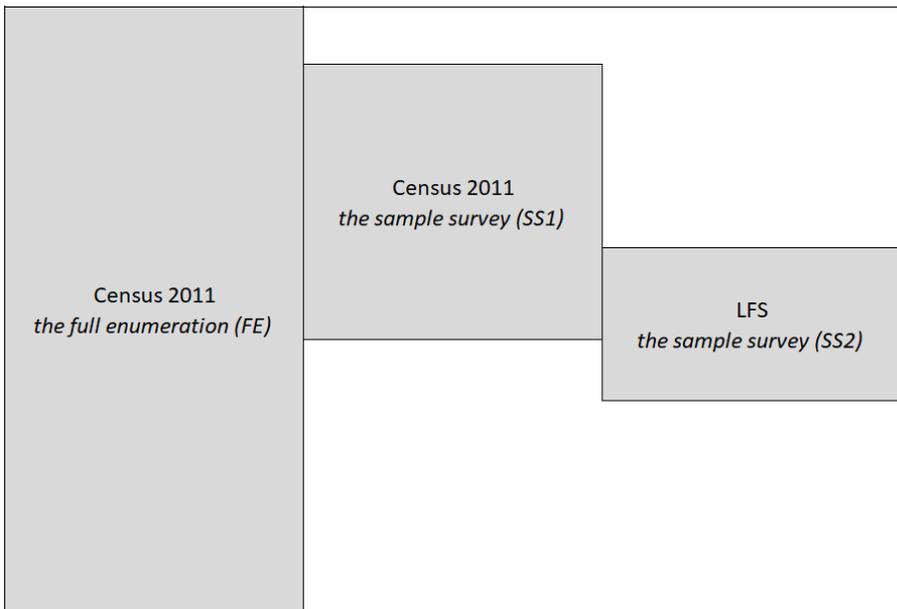


Figure 2. Integration of datasets from the NCPH and the LFS using probabilistic record linkage

Source: Own study.

3. The estimation procedure

Four blocks were extracted from the datasets obtained by integrating the NCPH and the LFS (see Figure 3). In Figure 3 block S_0 corresponds to the full enumeration in the NCPH—it covers the entire population and includes only those variables that were observed in the full enumeration in the NCPH. Block S_1 consists of respondents from the sample part of the NCPH and includes variables from both the full enumeration and the sample part of the NCPH. Block S_2 is an extension of the LFS dataset with variables from the full enumeration of the NCPH. Block S_3 is the common part of the sample part of the NCPH and LFS ($S_3 = S_1 \cap S_2$). On the one hand, S_3 is the smallest block in terms of the number of observations. On the other hand, it contains variables from all three surveys and therefore is the richest due to the scope of information.

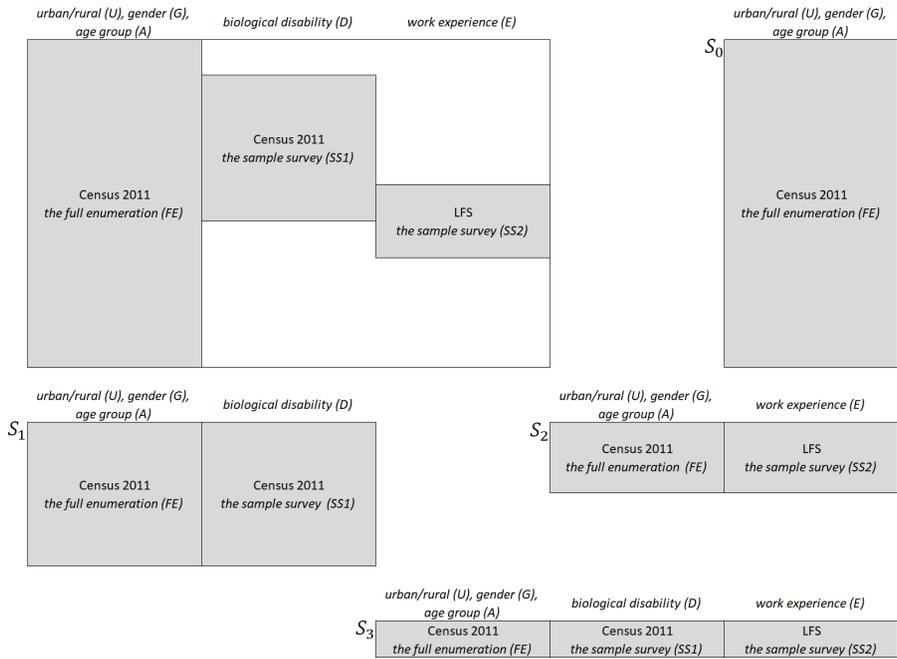


Figure 3. The construction of blocks based on integrated data from the NCPH and the LFS

Source: Own study.

According to the algorithm described above, the estimation of totals using the RW estimator is performed in the following three steps. In the first step, the final tables are defined, i.e. cross-classifications for which totals will be estimated. For illustrative purposes the following variables were used: urban /

rural (U), sex (G), age group (A), biological disability (D) and work experience (E). Their coding is presented in Table 1.

Table 1. Variables used for constructing the census tables

Variable	Symbol	Category	
urban/rural	U	1	urban
		2	rural
sex	G	1	male
		2	female
age group	A	1	15–17
		2	18–19
		3	20–24
		4	25–29
		5	30–34
		6	35–39
		7	40–44
		8	45–49
		9	50–54
		10	55–59
		11	60–64
		12	65+
biological disability ^a	D	1	yes
		2	no
work experience	E	1	yes
		2	no

^a Category 1 (yes) is assigned to people who reported biological disability, while Category 2 (no) applies to all others, which includes people who did not answer the question about biological disability. This method of coding and presentation of results was adopted by Statistics Poland.

Source: Own study.

The values of urban / rural, sex and age group variables are known for all respondents in the NCPH, while information on biological disability was collected only for respondents in the sample part of the NCPH and information regarding work experience is available only for LFS respondents.

In the presented example, we estimate table $D \times E \times G$ containing counts of people in cross-classifications defined by levels of biological disability, work experience and sex, as well as tables resulting from the aggregation of at

least one of its dimensions. The final set of tables to be estimated is as follows: $D, E, D \times E, D \times G, E \times G, D \times E \times G$.

The G table, containing counts of people by sex, is not estimated because it can be calculated by counting observations from the S_0 block covering the entire population. It should be noted that biological disability D and work experience E are not simultaneously observed in any of the surveys considered. Therefore, it is not possible to estimate $D \times E \times G$ and $D \times E$ based on one data source only. Hence, the S_3 block, which is a common part of the NCPH and the LFS, is used for this purpose.

In the second step, the totals contained in the tables defined in the first step are estimated based on the GREG estimator described in Section 1. Every table is estimated based on the most numerous block containing the variables defining the cross-classifications (see Table 2). As regards auxiliary information for the estimation process, a vector of indicator variables $\mathbf{x}_k^{UAG} = (x_{1,k}, \dots, x_{48,k})^T$ was used, which determines membership in one of the 48 groups defined by interactions of the following variables: urban / rural (U), sex (G) and age group (A)⁷.

Table 2. Final tables and corresponding blocks

Block	Output table
S_1	D
S_1	$G \times D$
S_2	E
S_2	$G \times E$
S_3	$D \times E$
S_3	$G \times D \times E$

Source: Own study.

The S_1 block was used to estimate the number of people by biological disability (D) as well as biological disability and sex ($D \times G$). For these domains, the following GREG estimators were used:

$$\hat{\tau}_D^{GREG(S_1)} = \hat{\tau}_D^{HT(S_1)} + \hat{\beta}_{S_1, D, UGA}^T (\tau_{UGA} - \hat{\tau}_{UGA}^{HT(S_1)}), \tag{10}$$

$$\hat{\tau}_{DG}^{GREG(S_1)} = \hat{\tau}_{DG}^{HT(S_1)} + \hat{\beta}_{S_1, DG, UGA}^T (\tau_{UGA} - \hat{\tau}_{UGA}^{HT(S_1)}), \tag{11}$$

where the final weights from the sample part of the NCPH were used as design weights $d_k^{(S_1)}$ ($k \in S_1$) with auxiliary variables defined as shown above.

⁷ This set of auxiliary variables was originally used in the process of weight calibration in the LFS by Statistics Poland.

The S_2 block was used to estimate totals by work experience (E) as well as work experience and sex ($E \times G$). *GREG* estimators for these tables are given by:

$$\hat{\boldsymbol{\tau}}_E^{GREG(S_2)} = \hat{\boldsymbol{\tau}}_E^{HT(S_1)} + \hat{\boldsymbol{\beta}}_{S_2, E, UGA}^T (\boldsymbol{\tau}_{UGA} - \hat{\boldsymbol{\tau}}_{UGA}^{HT(S_2)}), \quad (12)$$

$$\hat{\boldsymbol{\tau}}_{EG}^{GREG(S_2)} = \hat{\boldsymbol{\tau}}_{EG}^{HT(S_2)} + \hat{\boldsymbol{\beta}}_{S_2, EG, UGA}^T (\boldsymbol{\tau}_{UGA} - \hat{\boldsymbol{\tau}}_{UGA}^{HT(S_2)}), \quad (13)$$

where the original LFS weights were used as design weights $d_k^{(S_2)}$ ($k \in S_2$) along with auxiliary variables defined as shown above.

The S_3 block was used to estimate totals in domains defined by biological disability and work experience ($D \times E$) as well as biological disability, work experience and sex ($D \times E \times G$) using the following *GREG* estimators:

$$\hat{\boldsymbol{\tau}}_{DE}^{GREG(S_3)} = \hat{\boldsymbol{\tau}}_{DE}^{HT(S_3)} + \hat{\boldsymbol{\beta}}_{S_3, DE, UGA}^T (\boldsymbol{\tau}_{UGA} - \hat{\boldsymbol{\tau}}_{UGA}^{HT(S_3)}), \quad (14)$$

$$\hat{\boldsymbol{\tau}}_{DEG}^{GREG(S_3)} = \hat{\boldsymbol{\tau}}_{DEG}^{HT(S_3)} + \hat{\boldsymbol{\beta}}_{S_3, DEG, UGA}^T (\boldsymbol{\tau}_{UGA} - \hat{\boldsymbol{\tau}}_{UGA}^{HT(S_3)}). \quad (15)$$

The S_3 block is the common part of two sample surveys, hence input weights were determined as the product of weights from the sample part of the NCPH and LFS weights: $d_k^{(S_3)} = d_k^{(S_1)} d_k^{(S_2)}$ ($k \in S_3 = S_1 \cap S_2$). The same vector of auxiliary variables was selected.

By applying this approach separately for each of the S_i blocks ($i = 1, 2, 3$) one set of weights $w_k^{(S_i)}$ is obtained, which can then be used in the process of estimating totals as follows:

$$\hat{\boldsymbol{\tau}}_Y^{GREG(S_i)} = \sum_{k \in S_i} w_k^{(S_i)} \mathbf{y}_k, \quad (16)$$

where \mathbf{y}_k is a vector of indicator variables specifying the cross-classifications in the estimated table. The weights $w_k^{(S_i)}$ can be expressed using formula (5), where the S block is replaced with the S_i block and the vector of auxiliary variables is defined the same way as previously, i.e. $\mathbf{x}_k = \mathbf{x}_k^{UGA}$.

The use of one vector of weights $w^{(S_i)}$ in the given S_i block ensures consistency between the output tables estimated using this block. It is also easy to show that by using sex (G) as the auxiliary variable in the second step of the estimation process consistency was also achieved between tables estimated on the basis of the S_1 and S_2 blocks. Therefore, the estimates of totals in the domains: D , $D \times G$, E and $E \times G$ obtained using the estimators $\hat{\boldsymbol{\tau}}_D^{GREG(S_1)}$, $\hat{\boldsymbol{\tau}}_{DG}^{GREG(S_1)}$, $\hat{\boldsymbol{\tau}}_E^{GREG(S_2)}$, $\hat{\boldsymbol{\tau}}_{EG}^{GREG(S_2)}$ can be regarded as consistent. Therefore they will be treated as the final RW estimates.

A problem arises in the case of tables estimated from the S_3 block. If the counts of people by biological disability D and by work experience E were to be calculated by aggregating the appropriate totals contained in $\hat{\boldsymbol{\tau}}_{DE}^{GREG(S_3)}$ and

$\hat{\mathbf{t}}_{DEG}^{GREG(S_3)}$ results could be obtained that were different from the corresponding totals given by the estimate of $\hat{\mathbf{t}}_D^{GREG(S_1)}$ and $\hat{\mathbf{t}}_E^{GREG(S_2)}$. In order to avoid this potential inconsistency it is necessary to recalibrate the output tables.

The third step is performed in two stages (3a and 3b). In stage 3a, the GREG estimator is used again to ensure consistency between the following output tables: $D, E, D \times E$. A vector of auxiliary variables was constructed as follows:

$$\mathbf{x}_k^{D+E} = \underbrace{(x_{1,k}^D, x_{2,k}^D)}_{\mathbf{x}_k^D}, \underbrace{(x_{1,k}^E)}_{\mathbf{x}_k^{E^-}} \quad (17)$$

where $x_{1,k}^D$ takes the value 1, when the D variable for the k -th unit is the first category and 0 otherwise. The remaining indicator variables are defined in the analogous fashion. In order to avoid collinearity in \mathbf{x}_k^{D+E} , the variable $x_{2,k}^E$ was omitted. The weights $w_k^{(3)}$ from the second step were used as input weights. Finally, the estimates of $D \times E$ table were obtained using the following estimator:

$$\hat{\mathbf{t}}_{DE}^{RW} = \hat{\mathbf{t}}_{DE}^{GREG(S_3)} + \begin{pmatrix} \hat{\beta}_{w^{(3)}, DE, D} \\ \hat{\beta}_{w^{(3)}, DE, E^-} \end{pmatrix}^T \begin{pmatrix} \hat{\mathbf{t}}_D^{GREG(S_1)} - \hat{\mathbf{t}}_D^{GREG(S_3)} \\ \hat{\mathbf{t}}_{E^-}^{GREG(S_2)} - \hat{\mathbf{t}}_{E^-}^{GREG(S_3)} \end{pmatrix}. \quad (18)$$

The purpose of stage 3b was to ensure consistency between estimates in $D \times E \times G, D \times E, D \times G, E \times G$ tables. In this case, the vector of auxiliary variables was constructed as follows:

$$\mathbf{x}_k^{DG+EG^-+D^-E^-} = \underbrace{(x_{1,1,k}^{DG}, x_{1,2,k}^{DG}, x_{2,1,k}^{DG}, x_{2,2,k}^{DG})}_{\mathbf{x}_k^{DG}}, \underbrace{(x_{1,1,k}^{EG}, x_{2,1,k}^{EG})}_{\mathbf{x}_k^{EG^-}}, \underbrace{(x_{1,1,k}^{DE})}_{\mathbf{x}_k^{D^-E^-}} \quad (19)$$

where $x_{1,1,k}^{DG}$ is an indicator variable taking the value 1, when the k -th unit simultaneously has the first category of the D variable and the first level of the G variable, and 0 otherwise. The remaining indicator variables are defined in the analogous way. The weights $w_k^{(3)}$ from the second step were used as input weights. Finally, the estimator of table $D \times E \times G$ is given by:

$$\hat{\mathbf{t}}_{DE}^{RW} = \hat{\mathbf{t}}_{DE}^{GREG(S_3)} + \begin{pmatrix} \hat{\beta}_{w^{(3)}, DEG, DG} \\ \hat{\beta}_{w^{(3)}, DEG, EG^-} \\ \hat{\beta}_{w^{(3)}, DEG, D^-E^-} \end{pmatrix}^T \begin{pmatrix} \hat{\mathbf{t}}_{DG}^{GREG(S_1)} - \hat{\mathbf{t}}_{DG}^{GREG(S_3)} \\ \hat{\mathbf{t}}_{EG^-}^{GREG(S_2)} - \hat{\mathbf{t}}_{EG^-}^{GREG(S_3)} \\ \hat{\mathbf{t}}_{D^-E^-}^{GREG(S_3)} - \hat{\mathbf{t}}_{D^-E^-}^{GREG(S_3)} \end{pmatrix}. \quad (20)$$

The RW estimators described by formulas (18)–(20) are identical to calibration estimators given by:

$$\hat{\mathbf{t}}_{DE}^{RW} = \sum_{k \in S_3} r_k^{(S_3, 1)} \mathbf{y}_k \quad (21)$$

$$\hat{\tau}_{DEG}^{RW} = \sum_{k \in S_3} r_k^{(S_3,2)} \mathbf{y}_k \tag{22}$$

The weights $r_k^{(S_3,1)}$ and $r_k^{(S_3,2)}$ are given by formula (9), where the vectors of auxiliary variables \mathbf{m}_k are $\mathbf{x}_k^{D+E^-}$ and $\mathbf{x}_k^{DG+EG^-+D^-E^-}$ respectively, and inputs weights $w_k^{(S)}$ are weights $w_k^{(S_3)}$, obtained in the second step.

4. Results

Before applying the repeated weighting method, which consists of the three steps described above, a table containing the structure of the population aged 15+ by sex was constructed (see Table 3). It was constructed using data from the NCPH (full enumeration), i.e. was based on the S_0 block. Values in Table 3 do not have to be estimated because they can be obtained by simply counting observations (respondents) from the S_0 block covering the entire population. Such a table is constructed in order to verify the consistency of the row and column totals in the remaining tables, where sex is one of the variables.

Table 3. The structure of the population aged 15+ by sex (G)

G_1	G_2	Total
15,272,239	16,685,443	31,957,682

Source: Calculation based on integrated datasets from NCPH and LFS.

In the first step of applying the RW method the following tables were constructed: D , $D \times G$, E , $E \times G$, $D \times E$ and $D \times E \times G$ according to formulas (10)-(15) from the previous section. The totals estimated in the second step are presented in Tables 4-9. The margins for sex (G) and biological disability (D) in Table 5 ($D \times G$) and for sex (G) and work experience (E) in Table 7 ($E \times G$) are consistent with values shown in Tables 3, 4 and 6 (G , D and E). As noted earlier consistency issues arise with Tables 8 and 9 ($D \times E$ and $D \times E \times G$). The margins for biological disability (D) and work experience (E) are not consistent with those presented in Tables 4, 5, 6 and 7 (D , $D \times G$, E and $E \times G$). Consistency is only achieved in the case of sex (G), which results from its being used as one of the auxiliary variables in the estimation process.

Table 4. The structure of the population aged 15+ by biological disability (D)

D_1	D_2	Total
4,015,414	27,942,268	31,957,682

Source: Calculation based on integrated datasets from NCPH and LFS.

Table 5. The structure of the population aged 15+ by biological disability and sex ($D \times G$)

	D_1	D_2	Total
G_1	1,815,894	13,456,345	15,272,239
G_2	2,199,520	14,485,923	16,685,443
Total	4,015,414	27,942,268	31,957,682

Source: Calculation based on integrated datasets from NCPH and LFS.

Table 6. The structure of the population aged 15+ by work experience (E)

E_1	E_2	Total
27,399,998	4,557,684	31,957,682

Source: Calculation based on integrated datasets from NCPH and LFS.

Table 7. The structure of the population aged 15+ by work experience and sex ($E \times G$)

	E_1	E_2	Total
G_1	13,242,650	2,029,589	15,272,239
G_2	14,157,349	2,528,094	16,685,443
Total	27,399,999	4,557,683	31,957,682

Source: Calculation based on integrated datasets from NCPH and LFS.

Table 8. The structure of the population aged 15+ by biological disability and work experience ($D \times E$)—intermediate estimates obtained in the second step

	E_1	E_2	Total
D_1	3,881,336	234,662	4,115,997
D_2	23,529,766	4,311,919	27,841,685
Total	27,411,102	4,546,581	31,957,682

Source: Calculation based on integrated datasets from NCPH and LFS.

Table 9. The structure of the population aged 15+ by biological disability, work experience and sex ($D \times E \times G$)—intermediate estimates obtained in the second step

	E_1		E_2		Total
	G_1	G_2	G_1	G_2	
D_1	1,866,107	2,015,229	85,382	149,280	4,115,998
D_2	11,393,228	12,136,537	1,927,521	2,384,397	27,841,683
Total	13,259,335	14,151,766	2,012,903	2,533,677	31,957,681

Source: Calculation based on integrated datasets from NCPH and LFS.

In the third step of the repeated weighting algorithm, given the observed inconsistency between margins in the tables estimated in the second step, it was necessary to perform recalibration. As a result, the margins for biological disability (D) and work experience (E) in Tables 10 ($D \times E$) and 11 ($D \times E \times G$) match the values in Tables 4, 5, 6 and 7 (D , $D \times G$, E and $E \times G$ respectively). Also aggregations by $D \times E$ in Table 11 ($D \times E \times G$) are consistent with the values in Table 10 ($D \times E$).

Table 10. The structure of the population aged 15+ by biological disability and work experience ($D \times E$)—final estimates obtained in the third step

	E_1	E_2	Total
D_1	3,786,414	229,000	4,015,414
D_2	23,613,584	4,328,684	27,942,268
Total	27,399,998	4,557,684	31,957,682

Source: Calculation based on integrated datasets from NCPH and LFS.

Table 11. The structure of the population aged 15+ by biological disability, work experience and sex ($D \times E \times G$)—final estimates obtained in the third step

	E_1		E_2		Total
	G_1	G_2	G_1	G_2	
D_1	1,737,104	2,049,311	78,790	150,209	4,015,414
D_2	11,505,546	12,108,038	1,950,799	2,377,885	27,942,268
Total	13,242,650	14,157,349	2,029,589	2,528,094	31,957,682

Source: Calculation based on integrated datasets from NCPH and LFS.

Another important issue in the repeated weighting method is the way of assessing the estimation precision of totals in the output tables (see Table 12).

Table 12. Relative estimation errors of totals in the output tables

Table	Domain	<i>n</i>	REE(%)
<i>D</i>	D_1	2,647	0.1
	D_2	15,834	0.0
$D \times G$	$D_1 \times G_1$	1,221	0.2
	$D_1 \times G_2$	1,426	0.1
	$D_2 \times G_1$	7,442	0.0
	$D_2 \times G_2$	8,392	0.0
<i>E</i>	E_1	15,812	0.1
	E_2	2,669	0.6
$E \times G$	$E_1 \times G_1$	7,453	0.1
	$E_1 \times G_2$	8,359	0.1
	$E_2 \times G_1$	1,210	0.8
	$E_2 \times G_2$	1,459	0.8
$D \times E$	$D_1 \times E_1$	2,496	0.6
	$D_1 \times E_2$	151	9.6
	$D_2 \times E_1$	13,316	0.1
	$D_2 \times E_2$	2,518	0.8
$D \times E \times G$	$D_1 \times E_1 \times G_1$	1,162	2.2
	$D_1 \times E_1 \times G_2$	1,134	3.1
	$D_1 \times E_2 \times G_1$	59	48.9
	$D_1 \times E_2 \times G_2$	92	42.8
	$D_2 \times E_1 \times G_1$	6,291	0.7
	$D_2 \times E_1 \times G_2$	7,025	0.9
	$D_2 \times E_2 \times G_1$	1,151	4.1
	$D_2 \times E_2 \times G_2$	1,367	4.6

Source: Calculations based on integrated datasets from NCPH and LFS.

Table 12 presents relative estimation errors (REE) for all output tables, where estimator variance was evaluated using the method described by Knottnerus and van Duin (2006).⁸ In most cases, the obtained estimates are acceptable, with errors not exceeding 10%, except for estimates in table $D \times E \times G$ i.e.

⁸ Unfortunately, the applied approach does not take into account the randomness resulting from the stochastic method of data integration; hence the error measures presented in this article may be underestimated.

$D_1 \times E_2 \times G_1$ and $D_1 \times E_2 \times G_2$, for which exceeds this threshold. This is due to the small number of observations (59 and 92 respectively) used for estimating these totals.

Conclusions

The idea of the RW method is to ensure consistency of all final tables that created from various data sources supplying the census or to obtain numerically consistent estimates of tables from a combination of registers and surveys. The RW technique is based on repeated application of GREG and produces a new set of calibration weights for each table estimate. So far, it has been used successfully only by Statistics Netherlands in the regular estimation process to ensure consistency between different tables. Other National Statistical Offices, including Statistics Poland, in most cases use the calibration approach, which means that different systems of weights are used to produce tables based on different surveys.

In this study, the RW method was implemented based on data from NCPH and LFS from 2011. The goal was to construct tables defined by the status of biological disability, the work experience and sex. Thanks to the use of the RW method the following goals have been realised. First, this technique made it possible to construct a set of tables with consistent margins. This is, in fact, one of the most important goals in official statistics, which ensures that the end user obtains consistent data from various sources of information. Second, by combining information from many data sources, the RW method has been used to produce output tables that could not be obtained using only one source of information. This application has shown that the RW is particularly useful when the final tables have some variables in common.

Bearing in mind the advantages of the RW method and the fact that it has not been used so far in surveys carried out by Statistics Poland, the main goal of this article was to present the first application of this approach to real data from output tables. The use of the RW method and its testing on data from 2011 could pave the way for its implementation in the next Polish census scheduled for 2021 or in surveys where it is necessary to maintain consistency of estimates with results obtained from registers or other data sources.

References

- Boonstra, H. (2004). *A simulation study of repeated weighting estimation*. Voorburg/Heerlen: Statistics Netherlands.
- Boonstra, H., van den Brakel, J., Knottnerus, P., Nieuwenbroek, N., & Renssen, R. (2003). *Dacseis deliverable 7.2: A strategy to obtain consistency among tables of survey estimates*. Heerlen: Statistics Netherlands.

- Chambers, R., & Diniz da Silva, A. (2020). Improved secondary analysis of linked data: A framework and an illustration. *Journal of the Royal Statistical Society: Series A (Statistics in Society)*, 183(1), 37-59.
- De Waal, T. (2016). Obtaining numerically consistent estimates from a mix of administrative data and surveys. *Statistical Journal of the IAOS*, 32(2), 231-243.
- De Waal, T., van Delden, A., & Scholtus, S. (2020). Multi-source statistics: Basic situations and methods. *International Statistical Review*, 88(1), 203-228.
- Deville, J.-C., & Särndal, C.-E. (1992). Calibration estimators in survey sampling. *Journal of the American Statistical Association*, 87(418), 376-382.
- Harron, K., Goldstein, H., & Dibben, C. (2015). *Methodological developments in data linkage*. Hoboken: John Wiley & Sons.
- Haziza, D., & Lesage, É. (2016). A discussion of weighting procedures for unit nonresponse. *Journal of Official Statistics*, 32(1), 129-145.
- Houbiers, M. (2004). Towards a social statistical database and unified estimates at Statistics Netherlands. *Journal of Official Statistics*, 20(1), 55.
- Houbiers, M., Knottnerus, P., Kroese, A., Renssen, R., & Snijders, V. (2003). *Estimating consistent table sets: Position paper on repeated weighting*. (Statistics Netherlands, Discussion Paper, No. 3005).
- Kalton, G., & Flores-Cervantes, I. (2003). Weighting methods. *Journal of Official Statistics*, 19(2), 81.
- Knottnerus, P., & van Duin, C. (2006). Variances in repeated weighting with an application to the dutch labour force survey. *Journal of Official Statistics*, 22(3), 565.
- Kott, P. S. (2006). Using calibration weighting to adjust for nonresponse and coverage errors. *Survey Methodology*, 32(2), 133.
- Kott, P. S., & Chang, T. (2010). Using calibration weighting to adjust for nonignorable unit nonresponse. *Journal of the American Statistical Association*, 105(491), 1265-1275.
- Kroese, A., & Renssen, R. (1999). *Weighting and imputation at Statistics Netherlands*. (Proceedings of the IASS conference on Small Area Estimation, Riga August 1999, 109-120).
- Lundström, S., & Särndal, C.-E. (1999). Calibration as a standard method for treatment of nonresponse. *Journal of Official Statistics*, 15(2), 305.
- Luppés, M., & Nielsen, P. B. (2020). Micro data linking: Addressing new emerging topics without increasing the respondent burden. *Statistical Journal of the IAOS*, 1-13.
- Nordholt, E. S. (2005). The Dutch virtual census 2001: A new approach by combining different sources. *Statistical Journal of the United Nations Economic Commission for Europe*, 22(1), 25-37.
- Nordholt, E. S., van Zeijl, J., & Hoeksma, L. (2014). *Dutch Census 2011: Analysis and Methodology*. The Hague / Heerlen: Statistics Netherlands.
- R Core Team. (2019). *R: A language and environment for statistical computing*. Vienna: R Foundation for Statistical Computing.
- Rässler, S. (2012). *Statistical matching: A frequentist theory, practical applications, and alternative Bayesian approaches* (vol. 168). New York: Springer Science & Business Media.
- Renssen, R., Kroese, A., & Willeboordse, A. (2001). *Aligning estimates by repeated weighting*. Heerlen: Statistics Netherlands.

- Roszka, W. (2013). *Statystyczna integracja danych w badaniach społeczno-ekonomicznych*. (Unpublished doctoral dissertation). Poznań: Poznań University of Economics and Business.
- Särndal, C.-E. (2007). The calibration approach in survey theory and practice. *Survey Methodology*, 33(2), 99-119.
- Särndal, C.-E., & Lundström, S. (2005). *Estimation in surveys with nonresponse*. Hoboken: John Wiley & Sons.
- Sayers, A., Ben-Shlomo, Y., Blom, A. W., & Steele, F. (2016). Probabilistic record linkage. *International Journal of Epidemiology*, 45(3), 954-964.
- Statistics Poland. (2014). *The methodology of THE 2011 National Population and Housing Census: Selected aspects*.
- Szymkowiak, M. (2019). *Podejście kalibracyjne w badaniach społeczno-ekonomicznych*. Poznań: Wydawnictwo Uniwersytetu Ekonomicznego w Poznaniu.
- Van der Laan, J. (2018). *Reclin: record linkage toolkit*. R package version 0.1.1. Retrieved from <https://cran.r-project.org/web/packages/reclin/reclin.pdf>
- Wu, C. & Lu, W. W. (2016). Calibration weighting methods for complex surveys. *International Statistical Review*, 84(1), 79-98.
- Yang, S., & Kim, J. K. (2020). Statistical data integration in survey sampling: A review. *Japanese Journal of Statistics and Data Science*, 3, 625-650.
- Zhang, L.-C., & Tuoto, T. (2020). Linkage-data linear regression. *Journal of the Royal Statistical Society: Series A (Statistics in Society)*, 1-26.

Aims and Scope

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